ide dissolved in 1845.5 g . of 1.000 N hydrochloric acid. The equation yields the interpolated values in Table III.

## Heats of Formation

The data of Tables II and III are sufficient for obtaining the heat of formation of each calcium borate from the component oxides, care being taken to use the proper heat of solution value for boric oxide. For example, for the reaction 3 CaO $+\mathrm{B}_{2} \mathrm{O}_{3}$ (crystalline) $=3 \mathrm{CaO} \cdot \mathrm{B}_{2} \mathrm{O}_{3}, \Delta H_{298.16}=$ $3 \Delta H_{5}+\Delta H_{6}-\Delta H_{1}=-3 \times 46,380-3,286+$ $\$ 2,423=-60,000 \pm 40$ cal. per mole. Results, computed in this manner, are in Table IV.

## Table IV

| Heats of Formation (Cal. per Mole) |  |  |
| :---: | :---: | :---: |
| Substance | $\underset{\Delta H_{288.16}}{\text { From, }}$ | $\underset{\Delta H_{298-16}}{\text { From element }}$ |
| $3 \mathrm{CaO} \cdot \mathrm{B}_{2} \mathrm{O}_{3}$ | $-60000 \pm 40$ | -858200 |
| $2 \mathrm{CaO} \cdot \mathrm{B}_{2} \mathrm{O}_{3}$ | $-45760 \pm 30$ | -692100 |
| $\mathrm{CaO} \cdot \mathrm{B}_{2} \mathrm{O}_{3}$ | $-29420 \pm 20$ | -524000 |
| $\mathrm{CaO}-2 \mathrm{~B}_{2} \mathrm{O}_{3}$ | $-42930 \pm 20$ | -880200 |

To obtain the heats of formation from the elements (also in Table IV), there are needed the heats of formation of calcium and boric oxides. For the former, the result given by Bichowsky and Rossini ${ }^{13}$ is adopted, $\Delta H_{291}=-151,800$ cal. per mole; the error in assigning this value to
(13) Bichowsky and Rossini, "'Thermochemistry of Chemical Substances," Reinhold Publishing Corporation, New York, N. Y., 1936.
$298.16^{\circ} \mathrm{K}$. is inconsequential. Rossini ${ }^{14}$ has reevaluated Todd and Miller's ${ }^{15}$ heat of formation result for boric oxide glass, obtaining $\Delta H_{298.16}=$ $-338,400$ cal. per mole. Southard ${ }^{8}$ found $\Delta H_{298.16}=-4,360$ cal. per mole for the transformation of glassy boric oxide to crystalline boric oxide. Combining these figures, there is obtained $\Delta H_{298.16}=-342,760$ cal. per mole as the heat of formation of crystalline boric oxide. This value is used in deriving the column labelled "from elements" in Table IV. It is not possible at this time to assign precision uncertainties to values in this column.

It does not appear worthwhile to attempt to compare with heats of formation from the elements listed by Bichowsky and Rossini. ${ }^{13}$ Their results are based on a greatly different value for the heat of formation of boric oxide and on rather crude heat of solution measurements of the borates by Griveau. ${ }^{16}$

## Summary

Heats of solution of $3 \mathrm{CaO} \cdot \mathrm{B}_{2} \mathrm{O}_{3}, 2 \mathrm{CaO} \cdot \mathrm{B}_{2} \mathrm{O}_{3}$, $\mathrm{CaO} \cdot \mathrm{B}_{2} \mathrm{O}_{3}, \mathrm{CaO} \cdot 2 \mathrm{~B}_{2} \mathrm{O}_{3}, \mathrm{CaO}$ and $\mathrm{B}_{2} \mathrm{O}_{3}$ (crystalline) in 1.000 N hydrochloric acid were measured at $298.16^{\circ} \mathrm{K}$.

The results are used to obtain heats of formation of the four calcium borates from the component oxides and from the elements.
(14) Rossini, personal communication.
(15) Todd and Miller, This Journal, 68, 530 (1946).
(16) Griveau, Compt. rend., 166, 993 (1918).

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# High-Temperature Heat Contents of Uranium, Uranium Dioxide and Uranium Trioxide ${ }^{1}$ 

By G. E. Moore ${ }^{2}$ and K. K. Kelley ${ }^{3}$

In the autumn of 1942, the Pacific Experiment Station of the Bureau of Mines undertook the measurement of the high-temperature heat contents of uranium, uranium dioxide, and uranium trioxide, at the request of Professor H. C. Urey of Columbia University. The data were needed in connection with a then current National Defense Research Committee project and, as the Bureau of Mines had the only equipment for such measurements known to be in operating condition at the time, this arrangement was the most expeditious way of obtaining the desired values. The results of this work are the subject of the present paper. No previous, similar measurements of these three substances have been reported.

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## Materials

The materials came to us from E. A. Long, who was associated with Professor Urey at the time. The metal and the dioxide were of high purity but the trioxide required a purification treatment before use in the measurements.

The uranium sample consisted of two solid chunks of metal, semi-circular in cross-section, which together formed a circular cylinder of 1.3 cm . diameter and 1.3 cm . height. The uranium content, according to our analyses, was $99.71 \%$.

The uranium dioxide was in the form of powder and was composed of well-crystallized particles. Our analyses gave 88.26 per cent. uranium, as compared with the theoretical 88.15 per cent.
The uranium trioxide also was in powder form. As received, it contained $1.17 \%$ water not removable at $120^{\circ}$. This was determined by heating a weighed portion to $1,000^{\circ}$ and absorbing the expelled water in Dehydrite. The material
was purified by heating seventy-nine hours at 550 to $600^{\circ}$ in a stream of dry oxygen. During this period, a Dehydrite tube collected from the exit gas an amount of water corresponding to $1.15 \%$ of the weight of the sample, in substantial agreement with the above determination. The orange-yellow color of the material did not change noticeably during this treatment, indicating inappreciable decomposition. Final analyses gave $83.02 \%$ uranium, as compared with the theoretical $83.22 \%$.

## Measurements and Results

The heat contents were determined by the "drop" method in a previously described ${ }^{4}$ apparatus. The calorimeter was calibrated electrically in terms of the defined calorie ${ }^{5}$ ( $1 \mathrm{cal} .=4.1833$ int. joules).

The uranium was enclosed in silica-glass capsules during the measurements, the capsules having been sealed in an atmosphere of helium. Two series of measurements were made. In the first series, 30.476 g . of uranium was used and the silica capsule weighed 4.110 g . The second series was made with 30.467 g . of uranium in a $4.035-\mathrm{g}$. capsule. The heat content of the capsule in each instance averaged about $46 \%$ of the total measured heat content. Corrections for the capsules were made using the combined data of White, ${ }^{6}$ Southard, ${ }^{4}$ and Naylor ${ }^{7}$ for silica-glass. The possible uncertainty in the correction is large enough to produce a corresponding maximum uncertainty in the uranium results ranging from $1.5 \%$ at the lowest temperatures to $0.2 \%$ at the highest.

The uranium dioxide measurements were made with a $27.617-\mathrm{g}$. sample that was sealed by platinum welding in a platinum-rhodium capsule weighing 8.888 g . The heat content of the capsule, which was determined separately, averaged $15 \%$ of the total measured heat content.

The uranium trioxide measurements were made with a $20.698-\mathrm{g}$. sample, sealed by gold soldering in a 8.726 -g. platinum-rhodium capsule. The quantity of gold used in soldering was 0.112 g . The heat content of the capsule material was determined separately and available data ${ }^{8}$ were employed in computing the heat content of the small amount of gold. The combined heat contents of platinum-rhodium and gold comprised about $17 \%$ of the total measured heat content at all temperatures.

The results are assembled in Tables I, II and III, being listed in the order in which they were measured. Figure 1 shows the heat contents plotted against temperature.
(4) Southard, This Journal, 63, 3142 (1941).
(5) Mueller and Rossini, Am. J. Physics, 12, 1 (1944).
(6) White, Am. J. Sci., 47, 1 (1919); This Journal, 55, 1050 (1933).
(7) Kelley, Naylor and Shomate, Bur. Mines Tech. Paper, 686, 1946. 34 pp .
(8) Kelley. Bur. Mines Bull, 371 (1934) 78 pp.

Table I


Table II
High Temperature Heat Contents of Upanium Dioxide (Mol. Wt., 270.07)

| $T,{ }^{\circ} \mathrm{K}$. | $H_{\mathrm{T}}-, H_{295.16,}$ <br> cal./mole | $T,{ }^{\circ} \mathrm{K}$ | $H_{\mathrm{T}}-H_{285.15,}$ <br> cal./mole |
| :--- | :---: | :---: | :---: |
| 483.4 | 3175 | 1055.7 | 14440 |
| 484.2 | 3185 | 1068.3 | 14680. |
| 643.7 | 6185 | 1270.3 | 18875 |
| 662.1 | 6545 | 1269.9 | 18875 |
| 868.0 | 10615 | 758.8 | 8455 |
| 868.1 | 10615 | 1424.6 | 22170 |
| 965.9 | 12595 | 1462.5 | 22970 |

Table III
High-Temperature Heat Conteyts of Uranium Trioxide (Mol. Wt., 286.07)

| T, ${ }^{\circ} \mathrm{K}$. | $\begin{aligned} H_{\mathrm{T}}-H_{\text {298.1. }}, \\ \text { cal. } \end{aligned}$ | $T,{ }^{\circ} \mathrm{K}$. | $\underset{\text { cal./mole }}{H_{\mathrm{T}}-\underset{\text { mos.18 }}{ }}$ |
| :---: | :---: | :---: | :---: |
| 415.6 | 2440 | 700.8 | 8850 |
| 416.9 | 2450 | 775.9 | 10600 |
| 487.7 | 3985 | 805.4 | 11295 |
| 486.4 | 3995 | 867.0 | 12765 |
| 586.3 | 6200 | 885.6 | 13200 |
| 674.9 | 8260 | 576.2 | 5975 |

Nothing unusual was observed in the behaviot of the two oxides, but the metal exhibits two sharp transitions at $935 \pm 3^{\circ} \mathrm{K}$. and $1,045 \pm 3^{\circ} \mathrm{K}$., respectively. Results near the transition temperatures were accurately reproducible and there was no evidence of hysteresis. The heat and entropy of the $935^{\circ}$-transition are, respectively, $680 \mathrm{cal} . / \mathrm{g}$. atom and $0.73 \mathrm{cal} . / \mathrm{deg} . / \mathrm{g}$. atom. Corresponding values for the $1,045^{\circ}$-transition are $1,165^{\circ} \mathrm{cal} . / \mathrm{g}$. atom and 1.11 cal. $/ \mathrm{deg} . / \mathrm{g}$. atom.

The heat content results in Table I to III may be represented by the following relationships for which the temperature range of validity and mean deviation from the measured values are indicated in parentheses.
$\mathrm{U}(\alpha): H_{\mathrm{T}}-H_{298.16}=3.15 T+4.22 \times 10^{-3} T^{2}-0.80 \times$
$10^{5} T^{-1}-1046\left(298^{\circ}-935^{\circ} \mathrm{K} . ; 0.2 \%\right)$
$\mathrm{U}(\beta): H_{\mathrm{T}}-H_{298.16}=10.38 T-3525\left(935^{\circ}-1045^{\circ} \mathrm{K}\right.$,
$0.1 \%)$
$\mathrm{U}(\gamma): H_{\mathrm{T}}-H_{298.16}=9.10 T-1026\left(1045^{\circ}-1300^{\circ} \mathrm{K} . ;\right.$ $0.1 \%)$
$\mathrm{UO}_{2}: \quad H_{\mathrm{T}}-H_{288.16}=19.20 T+0.81 \times 10^{-3} T^{2}+3.957 \times$

$$
10^{5} T^{-1}-7124\left(298^{\circ}-1500^{\circ} \mathrm{K} \cdot i 0.1 \%\right)
$$

$\mathrm{UO}_{3}: \quad H_{\mathrm{T}}-H_{298.16}=22.09 T+1.27 \times 10^{-3} T^{2}+2.973 \times$
The heat content equations on differentiation yield the corresponding specific heat expressions listed
$\mathrm{U}(\alpha): C_{p}=3.15+8.44 \times 10^{-3} T+0.80 \times 10^{5} T^{-2}$
$\mathrm{U}(\beta): C_{P}=10.38$
$\mathrm{U}(\gamma): C_{p}=9.10$
$\mathrm{UO}_{2}: \quad C_{p}=19.20+1.62 \times 10^{-3} T-3.957 \times 10^{5} T^{-2}$
$\mathrm{UO}_{3}: \quad C_{p}=22.09+2.54 \times 10^{-3} \mathrm{~T}-2.973 \times 10^{5} T^{-2}$
Table IV gives even temperature values of the heat content and entropy increments above $298.16^{\circ} \mathrm{K}$. The former were read from smooth curves through the measured values. The latter were obtained by graphical integration of the measured values in the case of the metal and by integration of the heat content equations in the case of the oxides. The use of the equations for the oxides was justified as the maximum deviation from experimental values could alter the entropy at any temperature by only 0.01 unit at most.

Table IV
Heat Contents and Entropies above $298.16^{\circ} \mathrm{K}$.

| T, ${ }^{\circ} \mathrm{K}$. |  | $\begin{aligned} & S_{\mathrm{T}}-1 \\ & S_{288.16,} \\ & \text { cal./. } \\ & \text { deg./. } \\ & \text { mole } \end{aligned}$ | $\xrightarrow{-}$ |  | --- $\mathrm{UO}_{3}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $H_{\mathrm{T}}-$ $\mathrm{H}_{298.16}$, cal./ mole | $S_{T}-$ <br> $S_{298.16}$, cal. deg./ mole | $H_{T}-$ H298.16, mole | $S_{\mathrm{T}}$-- <br> $S_{298.18,}$ <br> cal. <br> deg.,' <br> nole |
| 400 | 690 | 1.98 | 1680 | 4.82 | 2090 | 6.01 |
| 500 | 1430 | 3.63 | 3470 | 8.82 | 4260 | 10.86 |
| 600 | 2240 | 5.10 | 5340 | 12.24 | 6510 | 14.96 |
| 700 | 3110 | 6.44 | 7280 | 15.22 | 8820 | 18.51 |
| 800 | 4060 | 7.71 | 9250 | 17.84 | 11160 | 21.64 |
| 900 | 5120 | 8.95 | 11250 | 20.21 | 13540 | 24.44 |
| 935 | $5500(\alpha)$ | 9.37 |  |  |  |  |
| 935 | 6180 ( $\beta$ ) | 10.10 |  |  |  |  |
| 1000 | 6855 | 10.80 | 13280 | 22.35 |  |  |
| 1045 | 7320 ( $\beta$ ) | 11.25 |  |  |  |  |
| 1045 | 8485 ( $\gamma$ ! | 12.36 |  |  |  |  |
| 1100 | 8985 | 12.83 | 15340 | 24.30 |  |  |
| 1200 | 9895 | 13.62 | 17420 | 26.11 |  |  |
| 1300 | 10805 | 14.35 | 19510 | 27.79 |  |  |
| 1400 |  |  | 21620 | 29.36 |  |  |
| 1500 |  |  | 23750 | 30.83 |  |  |

There are no previous data with which to compare any of these values. It may be of interest to note that the data indicate that the specific


Fig. 1.-High-temperature heat contents: A, uranium; $B$, uranium dioxide; $C$, uranium trioxide.
heat of the low-temperature modification of uranium increases from $6.57 \mathrm{cal} . / \mathrm{deg} . / \mathrm{g}$. atom at room temperature to 10.84 at $900^{\circ} \mathrm{K}$. Likewise, the indicated trend in the specific heat of the dioxide is from 15.2 to $21.4 \mathrm{cal} . / \mathrm{deg}$. $/ \mathrm{mole}$ in the range 298 to $1,500^{\circ} \mathrm{K}$. ; and for the trioxide, from 19.5 to $24.0 \mathrm{cal} . / \mathrm{deg}$./mole in the range 298 to $900^{\circ} \mathrm{K}$.

## Summary

High-temperature heat contents of uranium, uranium dioxide, and uranium trioxide were measured from 298.16 to $1,300,1,500$ and $900^{\circ} \mathrm{K}$., respectively.

Uranium undergoes two sharp transitions, at $935^{\circ} \pm 3^{\circ}$ and $1,045^{\circ} \pm 3^{\circ} \mathrm{K}$. The heats of transition are 680 and $1,165 \mathrm{cal} . / \mathrm{g}$. atom, respectively.

Equations representing the experimental results were derived and a table of heat content and entropy increments above $298.16^{\circ} \mathrm{K}$. was compiled. Berkeley, California Received April 9, 1947


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